

1 Euclidean Jordan algebras and inequalities on the parameters and on the spectra of a strongly regular graph

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Let τ be a strongly $(n, p; a, c)$ regular graph, such that $0 < c < p < n - 1$, A his matrix of adjacency and let \mathcal{V}_n be the Euclidean real space spanned by the powers of $A^j, j \in \mathbb{N}_0$ where the scalar product $\bullet|\bullet$ is defined by $x|y = \text{trace}(x \cdot y)$. In this work ones proves that \mathcal{V}_n is an Euclidean Jordan algebra of rank 3 when one introduces in \mathcal{V}_n the usual product of matrices. Working inside the Euclidean Jordan algebra \mathcal{V}_n with the the only complete system of orthogonal idempotents associated to A one defines the generalized krein parameters of the strongly $(n, p; a, c)$ regular graph τ . Finally one presents necessary conditions over the parameters and the spectra of the τ strongly $(n, p; a, c)$ regular graph.